



From Complexity to Intelligence

Machine Learning and Complexity





Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



Deduction vs Induction

What is the difference between deduction and induction ?





Deduction vs Induction

What is the difference between deduction and induction ?

Deductive reasoning is an approach where a set of logic rules are applied to general axioms in order to find (or more precisely *to infer*) conclusions of no greater generality than the premises. Inductive reasoning is an approach in which the premises provide **a strong evidence** for the truth of the conclusion.



Solomonoff's induction

What is the idea of Solomonoff's induction ?





Solomonoff's induction

What is the idea of Solomonoff's induction ?

Combining the **Principle of Multiple Explanations**, the **Principle of Occam's Razor**, **Bayes Rule**, using **Turing Machines** to represent hypotheses and **Algorithmic Information Theory** to calculate their probability.

$$H^* = \arg \max_{H_i} \left\{ 2^{-K(H_i)} \times Pr(D|H_i) \right\}$$





Proportional analogy

What is the problem of Proportional Analogy ?





Proportional analogy

What is the problem of Proportional Analogy ?

Definition (Analogy reasoning)

Analogy reasoning is a form of reasoning in which one entity is inferred to be similar to another entity in a certain respect, on the basis of the known similarity between the entities in other respects.

Proportional Analogy concerns any situation of the form “A is to B as C is to D”



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

 Unsupervised Learning

 Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



A basic approach of learning

A definition (T. Mitchell, 1997)

A computer program is said to learn from experience \mathcal{E} with respect to some class of tasks \mathcal{T} and performance measure \mathcal{P} , if its performance at tasks in \mathcal{T} , as measured by \mathcal{P} , improves with experience \mathcal{E} .





Examples

Handwriting recognition

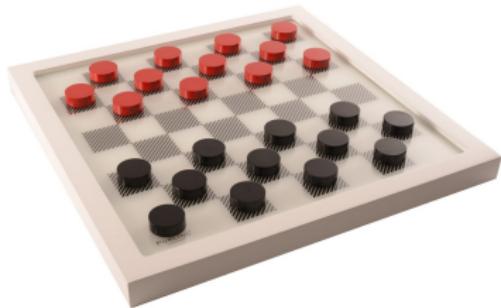


- **Task** : recognize and label handwritten words in images
- **Performance measure** : percentage of words successfully labeled
- **Experience** : database of manually labeled handwritten words



Examples

Checkers



- **Task** : play checkers
- **Performance measure** : percentage of victories
- **Experience** : practice games against itself



Examples

Video recommendation

The screenshot shows the Netflix homepage. At the top, there's a navigation bar with links for 'Watch instantly', 'Just for Kids', 'Personalized', 'DVDs', and a search bar. Below the navigation, it says 'Movies, TV shows, actors, directors' and shows a 'Aaron' profile icon. The main content area has two sections: 'Top 10 for Aaron' and 'Top TV Shows for Aaron'. Each section displays a grid of movie and TV show thumbnails. In the 'Top 10 for Aaron' section, the movies shown are 'The Minutemen', 'Random Hero', and 'Random Hero'. In the 'Top TV Shows for Aaron' section, the shows shown are 'Torchwood', 'Scandal', 'The Thin Blue Line', 'Heroes', 'The West Wing', and '24'.

- **Task** : recommend to any user videos he might like
- **Performance measure** : percentage of recommendation success
- **Experience** : list of videos liked by a set of users



A formal model

- **Input space** : a set \mathcal{X}
- **Output space** : a set \mathcal{Y}
- **Training data** : $\mathcal{D}_S = \{(x_1, y_1), \dots, (x_n, y_n)\}$
- **Decision function** : a function $h : \mathcal{X} \mapsto \mathcal{Y}$

Knowing the data \mathcal{D}_S , the system aims at learning the function h .



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

 Unsupervised Learning

 Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



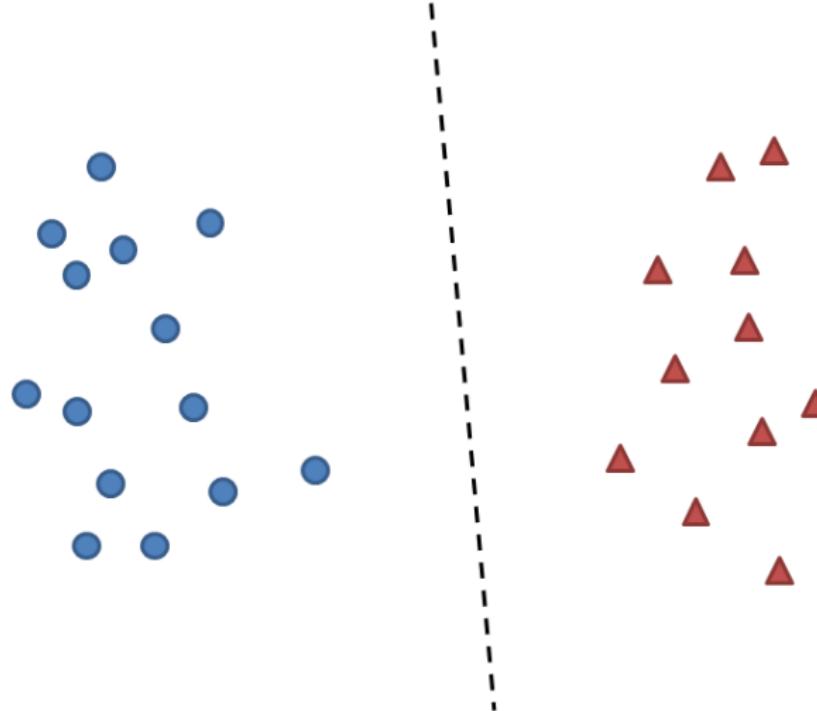
Supervised vs Unsupervised

- In **Supervised Learning**, the labels $y \in \mathcal{Y}$ are given. The goal is to estimate a correct labelling function $h : \mathcal{X} \mapsto \mathcal{Y}$.
- In **Unsupervised Learning**, the labels are unknown. The purpose is to group *similar* points.
- In **Semi-Supervised Learning**, some labels are unknown. The purpose is to estimate a correct labelling function h , exploiting information brought by non labelled points.



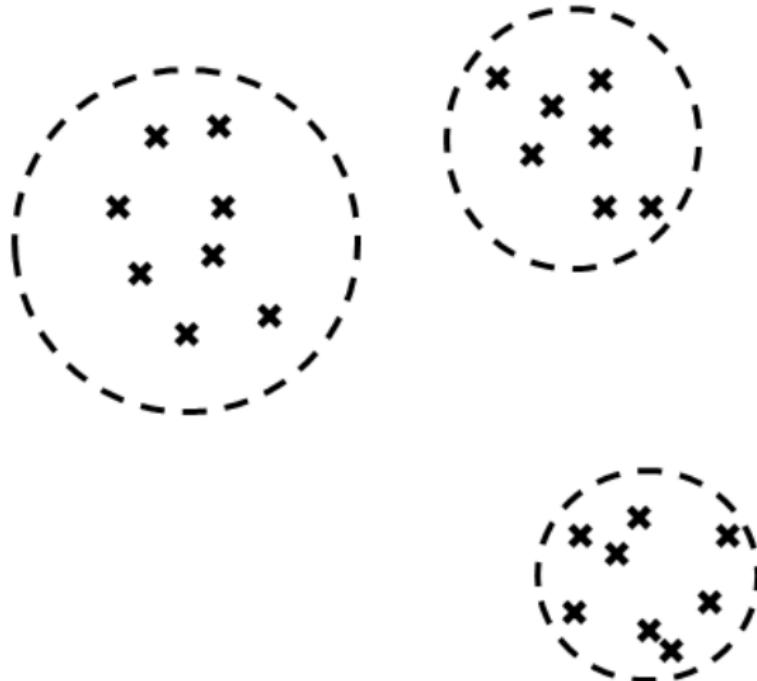
Supervised vs Unsupervised

Supervised Learning



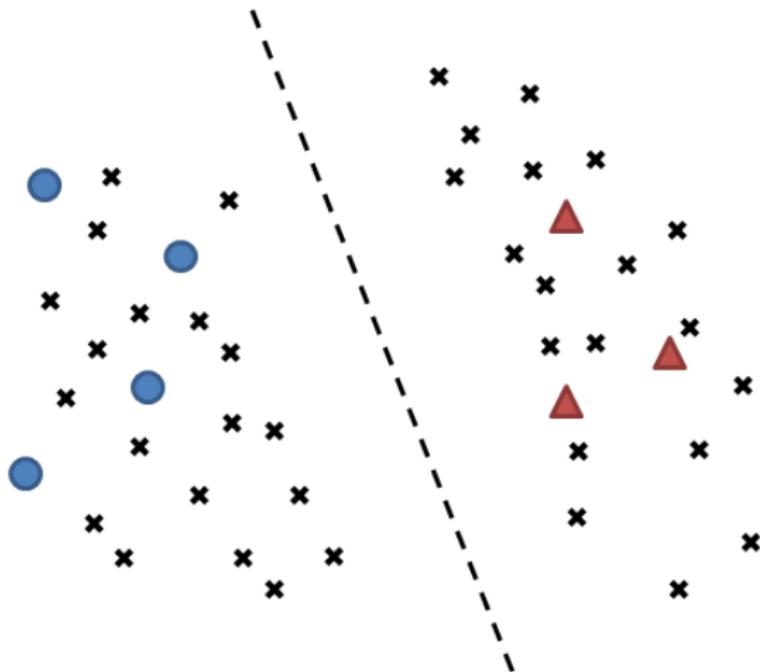


Supervised vs Unsupervised Unsupervised Learning





Supervised vs Unsupervised Semi-Supervised Learning





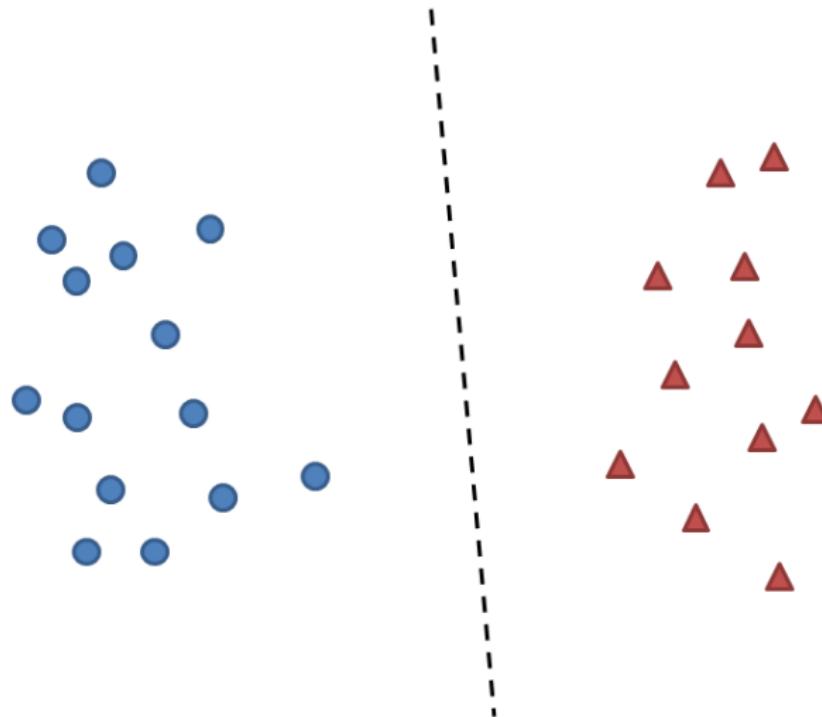
Classification vs Regression

- In **classification**, the output set \mathcal{Y} is discrete (and finite).
- In **regression**, the output set \mathcal{Y} is continuous.



Classification vs Regression

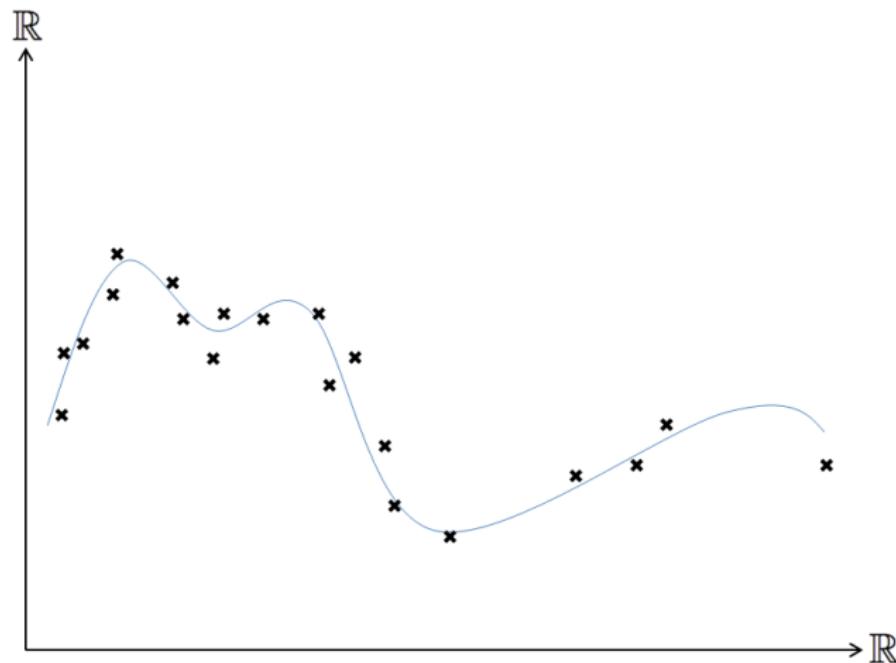
Classification





Classification vs Regression

Regression





Our objectives

We will :

- Focus on classification problems (mainly binary : $\mathcal{Y} = \{0, 1\}$)
- Consider Unsupervised Learning as a separate problem
- Examine what the statistics have to say
- Try to see a link with Analogy Reasoning



Our objectives

We will :

- Focus on classification problems (mainly binary : $\mathcal{Y} = \{0, 1\}$)
- Consider Unsupervised Learning as a separate problem
- Examine what the statistics have to say
- Try to see a link with Analogy Reasoning

We won't :

- Focus on methods
- Consider the problems of ranking and recommendation
- Consider “*real-time processes*”
- Pronounce the words *neural network* and *deep learning*



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



What is Unsupervised Learning ?

Reminder

In Unsupervised Learning, the learner receives unlabeled input data and aims at *finding a structure* for these data.

Tasks in Unsupervised Learning

- **Clustering** : grouping a set of objects such that similar objects end up in the same group and dissimilar objects are separated into different groups.
- **Anomaly detection** : identifying objects which do not conform to the global behavior.



Clustering



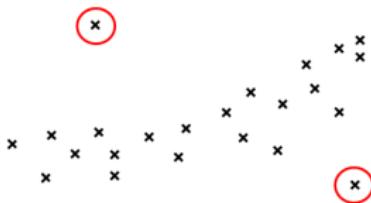
Basic idea : Points which are close are similar ;
Points which are far are dissimilar.

Applications :

- *Marketing* : detect groups of users with similar behaviors
- *Medicine* : detect mutations of a virus
- *Visualization* : find similar land-use on a satellite picture



Anomaly Detection



Basic idea : Find a general rule describing data and isolate points which do not obey this rule.

Applications :

- *Fraud detection*
- *Networks* : intrusion detection, event detection...



Unsupervised learning = Compression

Idea

In both Clustering and Anomaly Detection, the problem is to find regularities / structure.

Finding structure = Compressing the description of data

Hence, Unsupervised Learning = Compression

Besides, unsupervised learning is just a redescription of data, so is not directly a problem of induction.



Compression in Clustering

K-Means

K-Means algorithm

Inputs : Dataset $X = \{X_1, \dots, X_n\}$; Number of clusters k

Initialization : Randomly choose initial centroids μ_1, \dots, μ_k

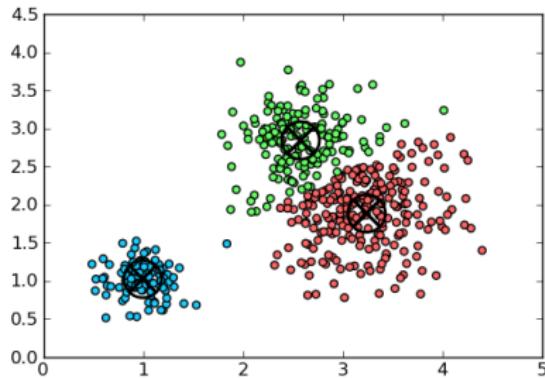
Repeat until convergence :

- For all $i \leq k$, set $C_i = \{x \in X; i = \operatorname{argmin}_j \|x - \mu_j\|\}$
- For all $i \leq k$, update $\mu_i = \frac{1}{|C_i|} \sum_{x \in C_i} x$



Compression in Clustering

K-Means



The data points are not described by their **absolute position** but by their **relative position to the closest prototype**.



Compression in Anomaly Detection

Applying MDL principle : find a model M minimizing $C(M) + C(D|M)$

x is an anomaly if $C(x|M) \approx C(x)$

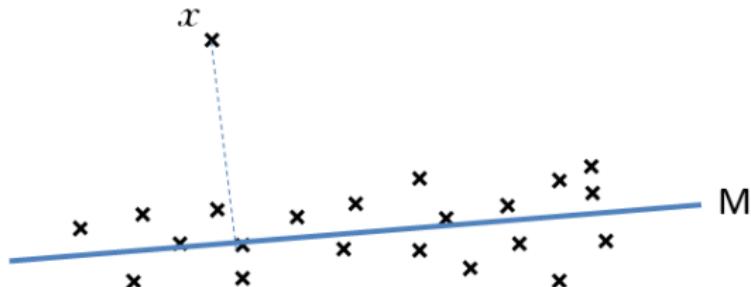




Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



A probabilistic notation

- Suppose that data $(X, Y) \in \mathcal{X} \times \mathcal{Y}$ are generated according to a probability distribution $\mathbb{P}_{X \times Y}$.
- Consider a *loss function* $l : \mathcal{Y} \times \mathcal{Y} \mapsto \mathbb{R}$ which quantifies the “cost” of misclassification
- We define the risk of a classifier $h : \mathcal{X} \mapsto \mathcal{Y}$ as :

$$R(h) = \int_{\mathcal{X} \times \mathcal{Y}} l(h(x), y) d\mathbb{P}_{X \times Y}(x, y)$$

- **Question** : can we find an algorithm which will *always* infer good hypotheses ?



The no-free-lunch theorem

Wolpert's answer



No !





The no-free-lunch theorem

[Wolpert, 1996]

For any two learning algorithms \mathcal{A}_1 and \mathcal{A}_2 with posterior distributions $p_1(h|\mathcal{S})$ and $p_2(h|\mathcal{S})$ (where \mathcal{S} is a data set), for any distribution $\mathbb{P}_{\mathcal{X}}$ of data and for any number m of data, the following propositions are true :

1. In uniform average over all target functions $f \in \mathcal{F}$:

$$\mathbb{E}_1[R|f, m] - \mathbb{E}_2[R|f, m] = 0$$

2. For any given learning set \mathcal{S} , in uniform average over all target functions $f \in \mathcal{F}$: $\mathbb{E}_1[R|f, \mathcal{S}] - \mathbb{E}_2[R|f, \mathcal{S}] = 0$

3. In uniform average over all possible distributions $P(f)$:

$$\mathbb{E}_1[R|f] - \mathbb{E}_2[R|f] = 0$$

4. For any given learning set \mathcal{S} , in uniform average over all possible distributions $P(f)$: $\mathbb{E}_1[R|\mathcal{S}] - \mathbb{E}_2[R|\mathcal{S}] = 0$



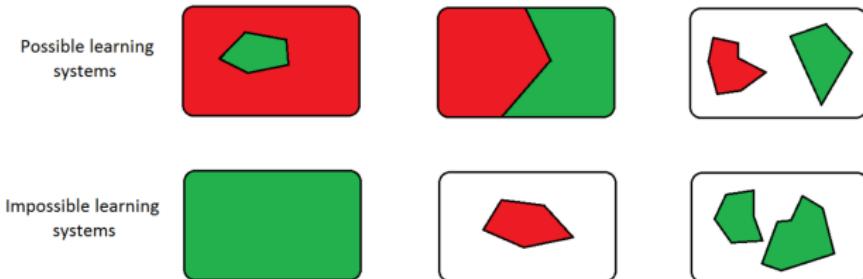


The no-free-lunch theorem

[Wolpert, 1996]

Consequences of the no-free-lunch theorem

- A “good” classification algorithm will have **in average** the same performance as a “bad” classification algorithm (*average over the space of problems*) if all target functions f are equiprobable.
- For any region of the space of problems where an algorithm \mathcal{A} is good, there exists a region where \mathcal{A} is bad.





Induction in Machine Learning

Conclusions of the no-free-lunch theorem

1. A learning algorithm is **biased** to a certain class of problems.
2. The performance of an algorithm is **necessarily** relative to a class of problems.
3. Induction does not create information : it only *transforms* a prior information contained in the algorithm.

There exists two types of biases :

1. **Representation bias** : a bias on the form of concept
2. **Research bias** : a bias on how the concept is searched



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



First principle : Empirical Risk Minimization

Given a loss function $l : \mathcal{Y} \times \mathcal{Y} \mapsto \mathbb{R}$ and a classifier h , we can define :

- The risk of h :

$$R(h) = \int_{\mathcal{X} \times \mathcal{Y}} l(h(x), y) d\mathbb{P}_{X,Y}(x, y)$$

- The empirical risk of h :

$$\widehat{R}_n(h) = \frac{1}{n} \sum_{i=1}^n l(h(x_i), y_i)$$

ERM principle : $\widehat{h} = \arg \min_h \widehat{R}_n(h)$



Second Principle : Bayesianism

Bayesianism is based on Bayes rule :

$$P(M|D) = \frac{P(M) \times P(D|M)}{P(D)}$$

■ Maximum A Posteriori (MAP) :

$$\hat{h}_{MAP} = \operatorname{argmax}_h \{ P(h|D) \times P(h) \}$$

■ Maximum Likelihood (ML) :

$$\hat{h}_{ML} = \operatorname{argmax}_h P(D|h)$$



Third Principle : Minimum Description Length

One more time !

MDL Principle

The best theory to describe observed data is the one which minimizes the sum of the description length (in bits) of :

- the theory description
- the data encoded from the theory

$$\hat{h} = \operatorname{argmin}_h K(h) + K(D|h)$$

or

$$\hat{h} = \operatorname{argmin}_h C(h) + C(D|h)$$



MDL and Bayesianism

Using the prefix complexity K , MDL principle is equivalent to Bayes rule :

$$K(h) + K(D|h) = -\log P(h) - \log P(D|h)$$

Thus :

$$\operatorname{argmin}_h \{K(h) + K(D|h)\} = \operatorname{argmax}_h \{\log P(h) + \log P(D|h)\}$$





Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



Reminder : the ERM principle

Given a loss function $l : \mathcal{Y} \times \mathcal{Y} \mapsto \mathbb{R}$ and a classifier h , we can define :

- The risk of h :

$$R(h) = \int_{\mathcal{X} \times \mathcal{Y}} l(h(x), y) d\mathbb{P}_{X,Y}(x, y)$$

- The empirical risk of h :

$$\widehat{R}_n(h) = \frac{1}{n} \sum_{i=1}^n l(h(x_i), y_i)$$

ERM principle : $\widehat{h} = \arg \min_h \widehat{R}_n(h)$



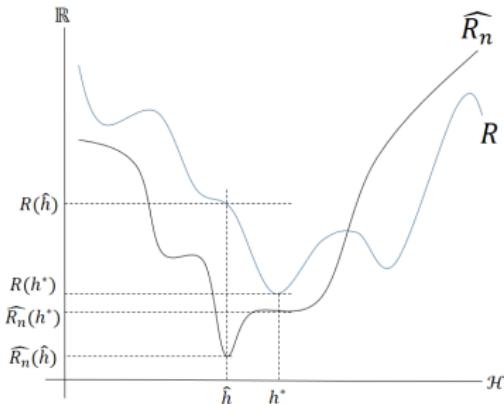
Is ERM legit ?

1. Is the hypothesis \hat{h} good in the real risk ?

$$\widehat{R}_n(\hat{h}) \xleftrightarrow{?} R(\hat{h})$$

2. Am I far from the real optimum ($h^* = \arg \min_h R(h)$) ?

$$R(\hat{h}) \xleftrightarrow{?} R(h^*)$$



Probabilities help us answer these questions.



Leslie Valiant (1949-...)

The purpose of PAC learning is to select **with high probability** (*probably*) a hypothesis **with low generalization error** (*approximately correct*).

PAC = Probably Approximately Correct



Is ERM legit ?

Step 1 :

Let's choose a classifier h with empirical risk $\widehat{R}_n(h) = 0$. What is the probability to have $R(h) > \epsilon$?

- Suppose that $R(h) \geq \epsilon$. The probability that **one** point is drawn with an empirical risk $\widehat{R}_1(h) = 0$ is :

$$p(\widehat{R}_1(h) = 0) \leq 1 - \epsilon$$

- After m **independent and identically distributed** draws :

$$p^m(\widehat{R}_n(h) = 0) \leq (1 - \epsilon)^m$$



Is ERM legit?

Step 1 :

For any $\epsilon, \delta \in [0, 1]$,

$$p^m(R(h) \geq \epsilon) \leq \delta \Leftrightarrow m \geq \frac{\ln\left(\frac{1}{\delta}\right)}{\epsilon}$$





Is ERM legit ?

Step 2 :

Let's choose our hypothesis in a finite set \mathcal{H} . Then for all $h \in \mathcal{H}, \delta \in [0, 1]$:

$$P^m \left[R(h) \leq \widehat{R}_m(h) + \frac{\ln |\mathcal{H}| + \ln \frac{1}{\delta}}{m} \right] > 1 - \delta$$

Oracle inequality :

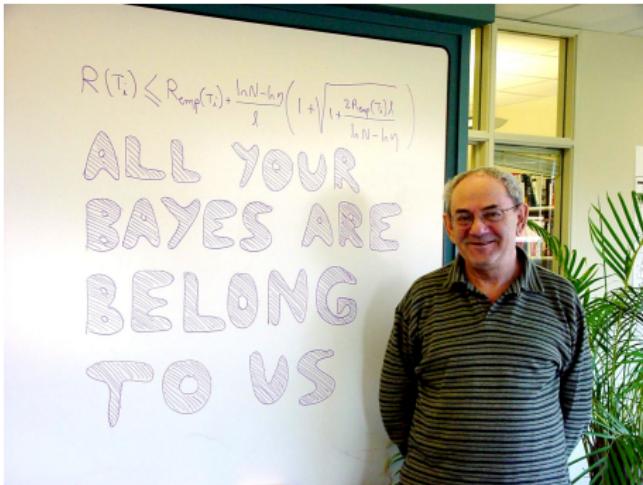
For any $\delta \in [0, 1]$:

$$P^m \left[R(\widehat{h}_m) \leq R(h^*) + \sqrt{\frac{2}{n} \ln \left(\frac{2|\mathcal{H}|}{\delta} \right)} \right] > 1 - \delta$$

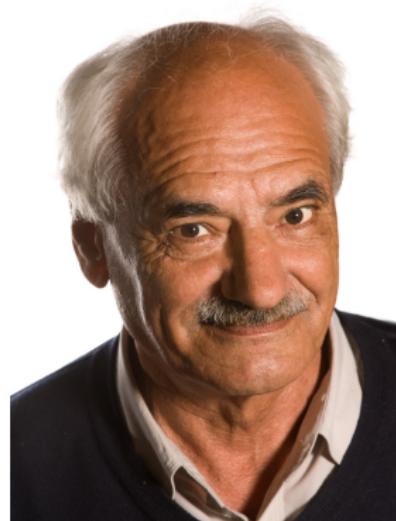


Is ERM legit?

Step 3 : What if the hypothesis space is infinite ?



Vladimir Vapnik (1936-...)



Alexei Chervonenkis (1938-2014)



Is ERM legit ?

Step 3 : What if the hypothesis space is infinite ?

Vapnik-Chervonenkis theory

Let \mathcal{H} be a Vapnik-Chervonenkis class. Then for any $\delta \in [0, 1]$:

$$P \left[R(\widehat{h}_m) \leq R(h^*) + 4\sqrt{\frac{2(V_{\mathcal{H}} \ln(m+1) + \ln 2)}{m}} + \sqrt{\frac{2 \ln \frac{1}{\delta}}{m}} \right] > 1 - \delta$$

and :

$$P \left[|R(\widehat{h}_m) - \widehat{R}_n(\widehat{h})| \leq 2\sqrt{\frac{2(V_{\mathcal{H}} \ln(m+1) + \ln 2)}{m}} + \sqrt{\frac{\ln \frac{1}{\delta}}{2m}} \right] > 1 - \delta$$





Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

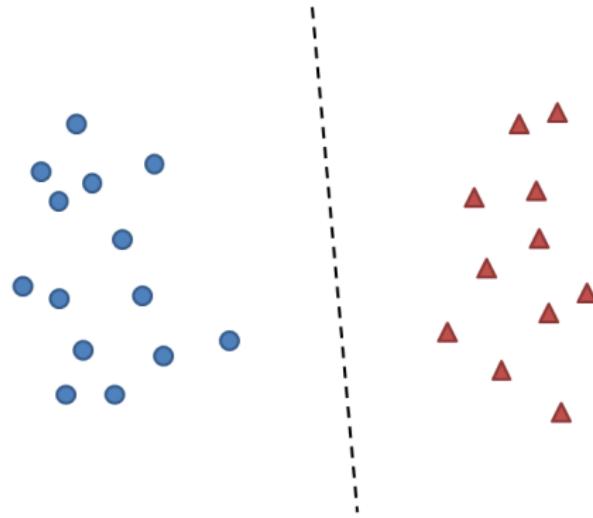
 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



Classification problem



Goal : find a *classifier* which “separates” the two classes.



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



Independent and Identically Distributed

In **statistical learning**, it is often assumed that data are i.i.d.
This assumption is **very strong and limiting** (but has really nice properties... !)

- **Independent** : $P(X_i, X_j) = P(X_i)P(X_j)$
- **Identically distributed** : The data X_i are drawn from a same distribution



Notations

- Data $\mathcal{D} = \{(X_1, Y_1), \dots, (X_n, Y_n)\}$
- Input space \mathcal{X} and output space \mathcal{Y}
- Hypothesis space \mathcal{H}
- A classifier is a function $h : \mathcal{X} \mapsto \mathcal{Y}$
- $h \in \mathcal{H}$





Basic MDL in i.i.d. setting

$$\text{minimize}_M \quad K(M) + K(X, Y|M)$$

$$\text{minimize}_M \quad C(M) + C(X, Y|M)$$

Generative approach :

- Aims at discovering the joint distribution of X and Y
- Gives a procedure to *generate* data from the same distribution
- The model describes the data

Discriminative approach :

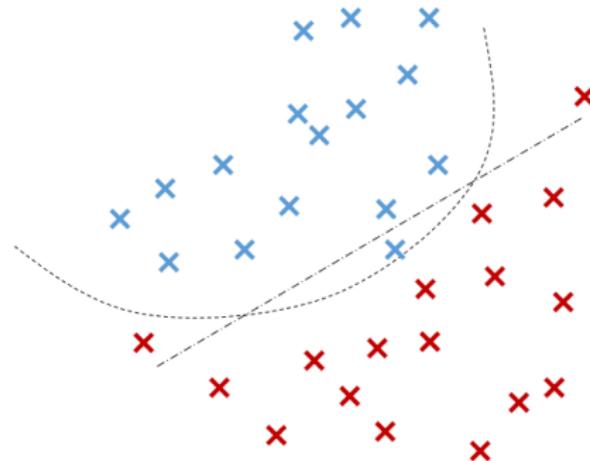
- Aims at discovering the conditional distribution of $Y|X$
- Gives a procedure to determine the classes
- The model does not describe the input data



MDL and model selection

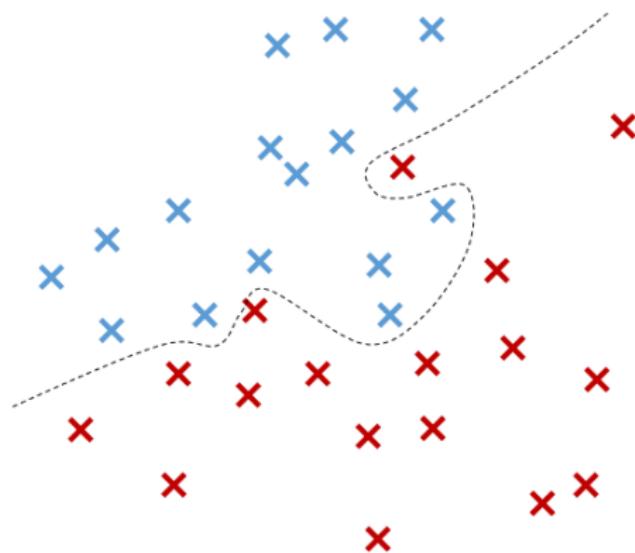
Main (admitted) use of MDL principle in Machine Learning !

If several models can explain the data, choose the model with the lowest Kolmogorov complexity.



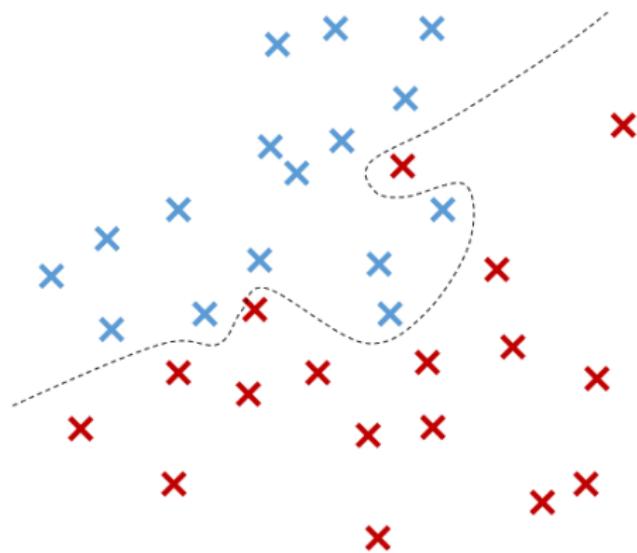


MDL and overfitting





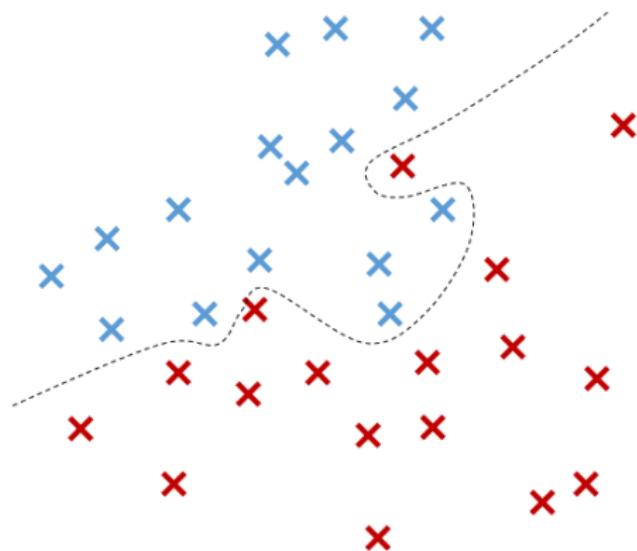
MDL and overfitting



MDL naturally prevents overfitting !



MDL and overfitting



MDL naturally prevents overfitting !
But was it intended... ?



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



From particular to particular

Back to Analogy Reasoning

ABC \implies ABD

IJK \implies ?





From particular to particular

Back to Analogy Reasoning

$$\mathbf{ABC} \implies \mathbf{ABD}$$

$$\mathbf{IJK} \implies ?$$

The problem can be formulated with the machine learning notations :

$$X_{learn} \implies Y_{learn}$$

$$X_{test} \implies ?$$

This problem has a name : **transfer learning**



From particular to particular

Transductive Learning

Statistics Professors HATE Him!



Doctor's discovery revealed the secret to learning any problem with just 10 training samples. Watch this shocking video and learn how rapidly you can find a solution to your learning problems using this one sneaky kernel trick! Free from overfitting!

<http://www.oneweirdkerneltrick.com>





From particular to particular

Transductive Learning

Solving a problem of interest, do not solve a more general (and therefore worse-posed) problem as an intermediate step. Try to get the answer that you really need but not a more general one.

- Do not estimate a density if you need to estimate a function. (*Do not use classical generative models ; use ML predictive models.*)
- Do not estimate a function if you need to estimate values at given points. (*Try to perform transduction, not induction*)
- Do not estimate predictive values if your goal is to act well. (*A good strategy of action can rely just on good selective inference.*)

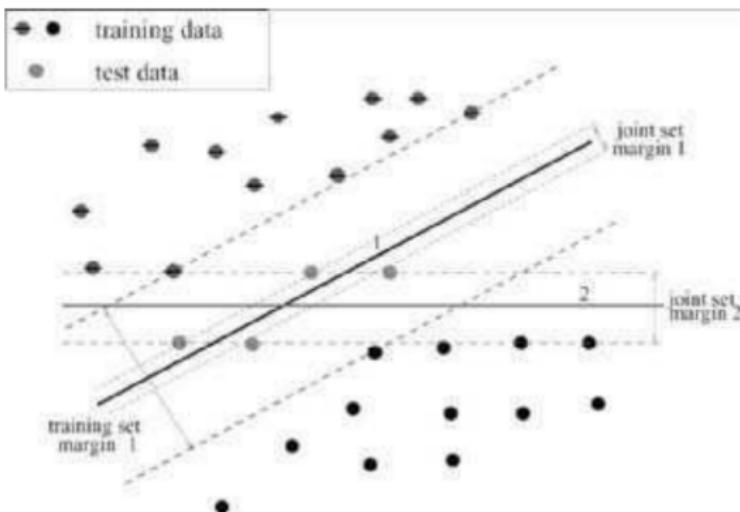




From particular to particular

Transductive Learning

Transduction = Transfer with i.i.d. hypothesis





From particular to particular

An equation (with familiar terms...)

$$\begin{aligned} C(M_S) + C(X_S|M_S) + C(\beta_S|M_S, X_S) + C(Y_S|M_S, X_S, \beta_S) \\ + C(M_T|M_S) + C(X_T|M_T) \end{aligned}$$





From particular to particular

An equation (with familiar terms...)

$$C(M_S) + C(X_S|M_S) + C(\beta_S|M_S, X_S) + C(Y_S|M_S, X_S, \beta_S) \\ + C(M_T|M_S) + C(X_T|M_T)$$

- $C(M)$: prior
- $C(X|M)$: likelihood
- $C(Y|M, X, \beta)$: risk
- $C(M_T|M_S)$: transfer term (related to a prior ?)





From particular to general

An intimidating gap

In many problems, I don't know the future test data ! Transduction is not possible... And our equation is not valid anymore...

- What does it mean *to generalize well* from a complexity point of view ?
- Is it enough to write that $X_T = \langle \rangle$?
- Our equation seems still valid (the individual terms are used in classical inductive principles.)



From particular to general

Answered questions ?

Isn't this question of generalization already answered by PAC learning,
VC theory etc... ?



From particular to general

Answered questions ?

Isn't this question of generalization already answered by PAC learning,
VC theory etc... ?

Yes and no !

These theories are valid only for the limit case of i.i.d. data **and i.i.d. questions**



From particular to general

Toward new principles ?

- 1. The learner is not indifferent to the future question** : the *priors* over the future are my only guarantee of generalization ?
- 2. All previously encountered data, problems and knowledge have a maximal pertinence** : Asymptotic results in statistical learning and Solomonoff's induction theories ? Creation of knowledge by one-shot learning ?



Table of contents

Reminder

Introduction to Machine Learning

 What is Machine Learning ?

 Types of Learning

Unsupervised Learning

Inductive Principles in Machine Learning

 The no-free-lunch theorem

 Three inductive principles

 Analysis of the ERM principle

Machine Learning and MDL Principle

 Basic MDL in i.i.d. setting

 Reaching generalization

Conclusion



What to remember ?

- Induction is **definitely not** a simple problem !
- Compression is closely related to learning
- The no-free-lunch theorem : no miracle classifier !
- MDL is hidden **everywhere** in Machine Learning
- New principles are necessary to formalize the transition from the particular to the general



What to remember ?

- Induction is **definitely not** a simple problem !
- Compression is closely related to learning
- The no-free-lunch theorem : no miracle classifier !
- MDL is hidden **everywhere** in Machine Learning
- New principles are necessary to formalize the transition from the particular to the general

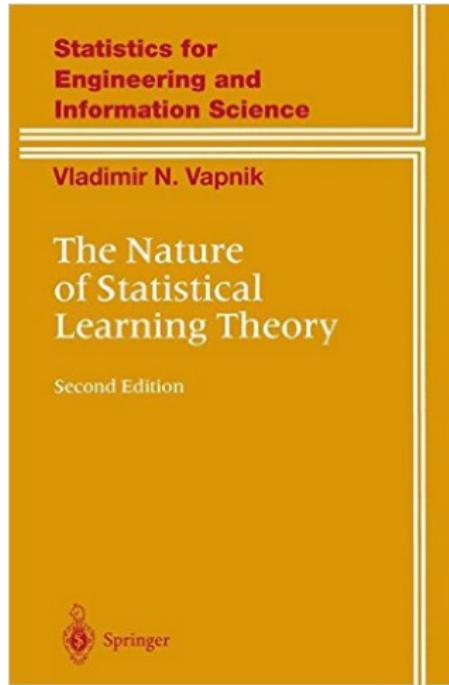
But...

- Most of these questions are never addressed in ML courses
- Most people prefer focusing on algorithms
- Most people ignore that such problems exist





If you are interested...





Licence de droits d'usage



Contexte public } sans modifications

Par le téléchargement ou la consultation de ce document, l'utilisateur accepte la licence d'utilisation qui y est attachée, telle que détaillée dans les dispositions suivantes, et s'engage à la respecter intégralement.

La licence confère à l'utilisateur un droit d'usage sur le document consulté ou téléchargé, totalement ou en partie, dans les conditions définies ci-après et à l'exclusion expresse de toute utilisation commerciale.

Le droit d'usage défini par la licence autorise un usage à destination de tout public qui comprend :

- Le droit de reproduire tout ou partie du document sur support informatique ou papier,
- Le droit de diffuser tout ou partie du document au public sur support papier ou informatique, y compris par la mise à la disposition du public sur un réseau numérique.

Aucune modification du document dans son contenu, sa forme ou sa présentation n'est autorisée.

Les mentions relatives à la source du document et/ou à son auteur doivent être conservées dans leur intégralité.

Le droit d'usage défini par la licence est personnel, non exclusif et non transmissible.

Tout autre usage que ceux prévus par la licence est soumis à autorisation préalable et expresse de l'auteur : sitedepedago@telecom-paristech.fr

